

## Transition from SAMO to Rydberg State Ionization in $C_{60}$ in Femtosecond Laser Fields

H. Li,<sup>†,‡</sup> B. Mignolet,<sup>§</sup> Z. Wang,<sup>†,||</sup> K. J. Betsch,<sup>†</sup> K. D. Carnes,<sup>†</sup> I. Ben-Itzhak,<sup>†</sup> C. L. Cocke,<sup>†</sup> F. Remacle,<sup>\*,§</sup> and M. F. Kling<sup>\*,†,⊥</sup>

<sup>†</sup>J. R. Macdonald Laboratory, Physics Department, Kansas State University, Manhattan, Kansas 66506, United States

<sup>‡</sup>State Key Laboratory of Precision Spectroscopy, East China Normal University, Shanghai 200062, China

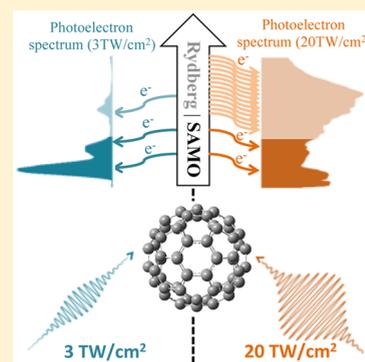
<sup>§</sup>Department of Chemistry, University of Liege, B-4000 Liege, Belgium

<sup>||</sup>The MOE Key Laboratory of Weak-Light Nonlinear Photonics, TEDA Applied Physics Institute and School of Physics, Nankai University, Tianjin 300457, China

<sup>⊥</sup>Department of Physics, Ludwig-Maximilians-Universität Munich, D-85748 Garching, Germany

### Supporting Information

**ABSTRACT:** The transition between two distinct ionization mechanisms in femtosecond laser fields at 785 nm is observed for  $C_{60}$  molecules. The transition occurs in the investigated intensity range from 3 to 20  $TW/cm^2$  and is visualized in electron kinetic energy spectra below the one-photon energy (1.5 eV) obtained via velocity map imaging. Assignment of several observed broad spectral peaks to ionization from superatom molecular orbitals (SAMOs) and Rydberg states is based on time-dependent density functional theory simulations. We find that ionization from SAMOs dominates the spectra for intensities below 5  $TW/cm^2$ . As the intensity increases, Rydberg state ionization exceeds the prominence of SAMOs. Using short laser pulses (20 fs) allowed uncovering of distinct six-lobe photoelectron angular distributions with kinetic energies just above the threshold (below 0.2 eV), which we interpret as over-the-barrier ionization of shallow f-Rydberg states in  $C_{60}$ .



Studying ultrafast electronic and nuclear dynamics in complex systems has become a key research field in recent years.<sup>1–9</sup> Among the large variety of target systems, the  $C_{60}$  fullerene has been an archetypical nanoscale system for the investigation of many-body problems.  $C_{60}$  exhibits hybrid properties that bridge the gap between molecular and bulk systems and has a complex response to laser excitation. The behavior of  $C_{60}$  in femtosecond (fs) laser fields usually exhibits an interplay of single-active-electron dynamics in atoms and a multiactive-electron response of polyatomic molecules.<sup>10–13</sup> Furthermore, external fields can lead to strong coupling of electronic and nuclear degrees of freedom.<sup>14</sup> The ionization and fragmentation of  $C_{60}$  have been investigated with tailored laser pulses.<sup>15–17</sup> It was found that the response of  $C_{60}$  to intense laser pulses heavily depends on pulse duration. When excited by ns laser pulses, delayed ionization on microsecond time scales can be observed, which arises from efficient energy redistribution between the electronic and vibrational degrees of freedom.<sup>16,18</sup> In fs laser fields (down to tens of fs), prominent peak structures can be observed superimposed on a “thermal” background.<sup>19,20</sup> Within time scales of about 100 fs, the excitation energy mostly remains in electronic degrees of freedom, yielding emitted photoelectrons with a much higher effective temperature compared to those obtained in ps laser fields, where significant energy can be transferred to vibrations.<sup>14,19,21</sup> The nature of electron emission has been

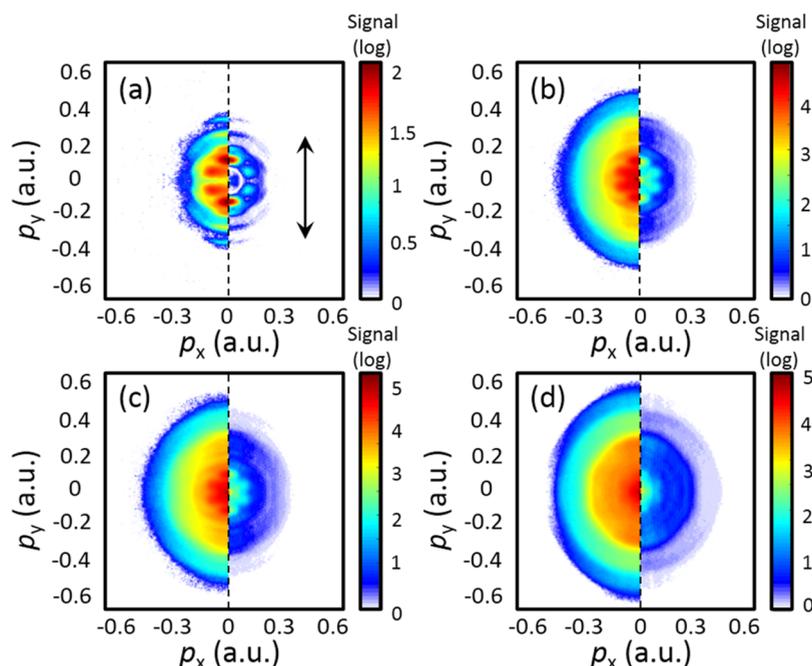
shown to depend on laser fluence for femtosecond pulses at moderate intensities.<sup>14,19</sup> Earlier work assigned peaks to ionization from a series of Rydberg states (with  $n = 3, 5, 7$ ).<sup>11</sup> Recently, electronic states arising from excitation of atomic-like molecular orbitals, in which the electronic density is localized both inside and outside of the fullerene cage and that exhibit the nodal patterns of nanometric size hydrogenic orbitals, have been discovered in  $C_{60}$  molecules adsorbed on copper surfaces with scanning tunneling microscopy (STM).<sup>22,23</sup> These states were named SAMOs for superatom molecular orbitals. They also have been characterized for isolated gas-phase  $C_{60}$  molecules using photoelectron imaging techniques.<sup>24</sup>

The properties of SAMO states in fullerenes are of interest for designing nanodevices because they can form nearly free electron bands in solids.<sup>23</sup> Exploring SAMO states in the gas phase provides an approach that is free of molecule–substrate interactions and therefore is more easily compared with theoretical results. Systematic theoretical studies of the excited electronic states of  $C_{60}$  based on time-dependent density functional theory (TDDFT) have revealed that the SAMO excited states differ from the Rydberg states in many aspects.<sup>25</sup>

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**Figure 1.** (a–d) Momentum distributions of the photoelectron emission from  $C_{60}$  in a 20 fs laser field at intensities of 3.0, 7.5, 10, and 20  $TW/cm^2$ , respectively. The uncertainty for the intensity is about 10%. Raw VMI images are shown in the left half. The images in the right half are Abel-inverted and correspond to the 2-D momentum distributions around the  $p_z = 0$  plane. The laser is polarized along the  $y$ -axis, as indicated by the arrow in (a).

The SAMO excited states have a significant electronic density inside of or in close vicinity to the fullerene cage, whereas the charge density for Rydberg orbitals localizes tens of Å outside of the fullerene cage. The density inside of the cage stabilizes the excited states, generating low-lying SAMO excited states. SAMO and Rydberg states are also characterized by markedly different photoionization rates.<sup>25</sup> Therefore, their photoionization lifetimes, which represent the time that it takes an electronic state population to ionize with a yield of 63% ( $1 - 1/e$ ) through the interaction with the pulse electric field, are also markedly different.

While both SAMO and Rydberg states have been observed for photoexcited gas-phase  $C_{60}$  molecules,<sup>10,24</sup> studies of their relative contribution to the photoelectron spectra (PES) as a function of laser intensity have been hampered by a background of thermal electron emission for longer pulses (of about 100 fs and above). Here, we used 20 fs near-infrared (NIR) laser pulses centered at 785 nm to circumvent this problem and selectively photoionize SAMO or Rydberg states in  $C_{60}$  by tuning the laser intensity. The intensity dependence of the resulting PES clearly shows the transition between ionization of SAMO and Rydberg states for the studied intensity range of 3–20  $TW/cm^2$ . Furthermore, the low background in thermal electron emission allowed uncovering of a six-lobe angular distribution at low kinetic energies, the origin of which is illuminated with our calculations.

The experimental setup is introduced in detail in the Supporting Information (SI). Briefly, a beam of 20 fs pulses at a central wavelength of 785 nm is focused into a velocity map imaging (VMI) spectrometer, where it intersects a beam of neutral  $C_{60}$  molecules generated from a homemade oven. The laser intensity is adjusted by a rotatable neutral density filter. The 3-D momentum distributions of the resulting photoelectrons after laser–fullerene interaction are measured with the VMI and postprocessed by Abel inversion<sup>26</sup> to extract the 2-D momentum distribution in the plane around  $p_z = 0$ , where

the laser is polarized along the  $y$ -axis and propagating along the  $x$ -axis (see the SI). The peak intensities in the focal volume are estimated by measuring the above-threshold ionization (ATI) electron emission from Xe under identical experimental conditions.<sup>27</sup>

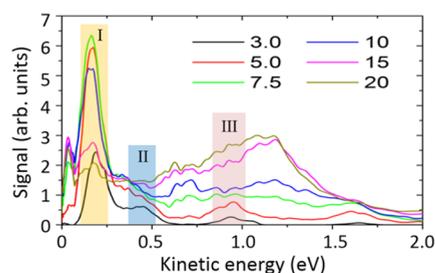
The theoretical interpretation of the PES is based on the computed values of binding energies and photoionization lifetimes of 17 bands of SAMO and Rydberg states. The SAMO states are not optically active; therefore, they cannot be accessed directly from the ground state. Several mechanisms including vibronic coupling to optically active valence states, which is estimated to take 50–100 fs,<sup>16,18</sup> and dipole coupling between optically active and dark excited states can lead to the population of the SAMO and Rydberg states during the pulse (see the SI for more details). The SAMO and Rydberg states also have large dipole coupling with the p-SAMO states that are in turn vibronically coupled to quasi-isoenergetic bright valence states. Modeling the electron–nuclear dynamics, required to describe the photoexcitation or vibronic coupling during the pulse, is currently out of reach for a large molecule such as  $C_{60}$ . Therefore, we do not attempt to explicitly describe the dynamics of the photoexcitation process here. Once the SAMO and Rydberg states are transiently populated during the pulse, they can be ionized by one-photon ionization, leading to sharp peaks in the PES spectrum or by over-the-barrier ionization (OTB) if the lowering of the ionization potential (IP) due to the Stark shift is larger than the binding energy of the states so that they become metastable.

The electronic structure required for the computation of the binding energies and photoionization lifetimes of the SAMO and Rydberg states is carried out at the TDDFT level using the 6-31G(d) basis set augmented by a set of 12 diffuse atomic orbitals of s, p, d, and f symmetry to account for the very diffuse s, p, d, and f-Rydberg states close to the IP. The band of excited electronic states was limited to 500 states by restricting the number of allowed transitions to the excited states.<sup>28</sup> The LC-

BLYP functional was used with a tuned parameter of 0.21 (ref 29) so that the Rydberg series converged to the IP. The computed binding energies of the Rydberg states are in good agreement with the Rydberg series of  $C_{60}$  (ref 10) with a quantum defect of 0.84 (ref 30). From the electronic states, we computed the photoionization lifetimes and angular distributions.<sup>25,31,32</sup> The lifetimes depend on the orbital from which the electron is ionized (i.e., the Dyson orbital), on the kinetic energy of the ionized electron (given by the difference between the IP of the ionized state and the energy of the photon), and on the field strength of the laser. The lifetimes strongly depend on the properties of the Dyson orbitals, in particular, their nodal patterns and diffuse character. The SAMO and Rydberg states have Dyson orbitals<sup>25,31,33</sup> with a simple hydrogenic electron distribution and a few nodes, which results in large photoionization coupling elements and small lifetimes. In comparison, for the same kinetic energy and laser intensity, the lifetimes of SAMO and Rydberg states are more than 3 orders of magnitude lower than the ones of the valence excited states. Photoionization lifetimes sharply increase with photoelectron kinetic energy for the SAMO and Rydberg states.<sup>25,34</sup> Because the SAMOs have larger binding energies than Rydberg states, the kinetic energy of the ionized electron corresponding to the one-photon photoionization of a SAMO electronic state is lower, and therefore, its lifetime is shorter. The lifetimes are computed for a laser intensity corresponding to the maximum of the laser pulse. However, the laser only reaches its maximum intensity during a limited time, so that only the electronic states with a lifetime much smaller than the pulse duration will ionize during the pulse. Once the pulse is over, the states are stable because they are below the IP and therefore they cannot ionize, except by tunnelling ionization, which is a much slower process.

The momentum distributions of the photoelectron emission from  $C_{60}$  are measured at several laser intensities in the range of 3–20  $\text{TW}/\text{cm}^2$ . Four corresponding VMI images are shown in Figure 1a–d. The raw VMI images are shown on the left and the Abel-inverted images on the right half. Rich information can be extracted from these VMI images. First, characteristic peaks from ATI electron emission with spacing equal to the photon energy can be observed for radial momenta  $p_r > 0.3$  a.u.,  $p_r = \sqrt{p_x^2 + p_y^2}$ . ATI electron emission in  $C_{60}$  has been investigated for various pulse durations down to sub-10 fs.<sup>16</sup> The reducing contrast and smoothing of the angular distribution of the ATI peaks with increasing laser intensity can be attributed to many-electron effects in ultrafast ionization of  $C_{60}$  (ref 13).

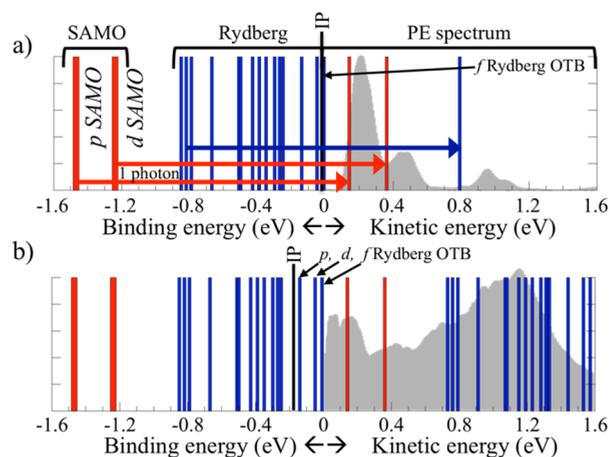
We focus here on the momentum range  $p_r < 0.3$  au (which corresponds to the energy range in the PES shown in Figure 2



**Figure 2.** PES for different laser intensities (indicated numbers are in units of  $\text{TW}/\text{cm}^2$ ) obtained from integration over Abel-inverted experimental VMI images.

below 1.5 eV). The PES along the laser polarization axis are obtained by integrating the signal along the  $p_y$  axis within an angular range of  $\pm 10^\circ$  and are shown in Figure 2 for the indicated laser intensities (in units of  $\text{TW}/\text{cm}^2$ ). For the lowest intensity, that is, 3.0  $\text{TW}/\text{cm}^2$ , three distinct peaks can be distinguished below the one-photon energy. They are around 0.2, 0.5, and 1.0 eV (marked with Peak I, II, and III), with the peak height decreasing for higher kinetic energies and the peak at 0.2 eV dominating.

On the basis of the binding energies and photoionization lifetimes, we assign the first peak to the p-SAMO, the second one to the d-SAMO, and the third one to the 2p-Rydberg states. The kinetic energy of the peaks corresponds qualitatively to the one-photon ionization of the p- and d-SAMOs and 2p-Rydberg states computed at the TDDFT level (see Figure 3a).



**Figure 3.** Binding energy of the SAMO and Rydberg states (left) and the experimental photoelectron spectrum (right) for laser intensities of 3 (a) and 20  $\text{TW}/\text{cm}^2$  (b). In both panels, a bar corresponding to the kinetic energy of the ionized electron is shown when the one-photon photoionization lifetime of an electronic state is shorter than 10 fs. The IP lowered by the Stark shift (0.02 and 0.21 eV for intensities of 3 and 20  $\text{TW}/\text{cm}^2$ , respectively) is shown by a black bar. All of the states above the lowered IP that can photoionize by the OTB mechanism are indicated. The values of the OTB lifetimes have not been computed.

The excitation energy and, therefore, the kinetic energy of the ionized electron for the SAMO and Rydberg states are systematically underestimated by 0.1–0.2 eV compared to the experiment, as expected in TDDFT.<sup>35</sup> Furthermore, the assignment of the p- and d-SAMO agrees with former work<sup>10,11,24</sup> (within 0.1 eV). Among the dense manifold of SAMO and Rydberg states, only the three states listed in Table 1 have a photoionization lifetime shorter than 10 fs for an intensity of 3  $\text{TW}/\text{cm}^2$ , such that they dominate the PES. The other excited states can be populated during the pulse, but they will not photoionize significantly during its  $\sim 20$  fs duration because of their longer lifetimes. The computed average lifetime of the Rydberg states is around 40 fs (Table 1). The relative height of the peaks is governed by the excitation process that is not modeled here. The computed value of the lifetimes only allows determining if the electronic state can ionize or not during the pulse.

As the laser intensity increases, a contribution in the spectrum at around 0.7 eV appears. For higher laser intensities, a broad peak between 1.0 and 1.5 eV becomes more intense and dominates the spectrum. This peak reflects the ionization

**Table 1. Lifetimes (in fs) of  $C_{60}$ 's p-SAMO, d-SAMO, and 2p-Rydberg States for the Lowest and Highest Applied Intensities<sup>a</sup>**

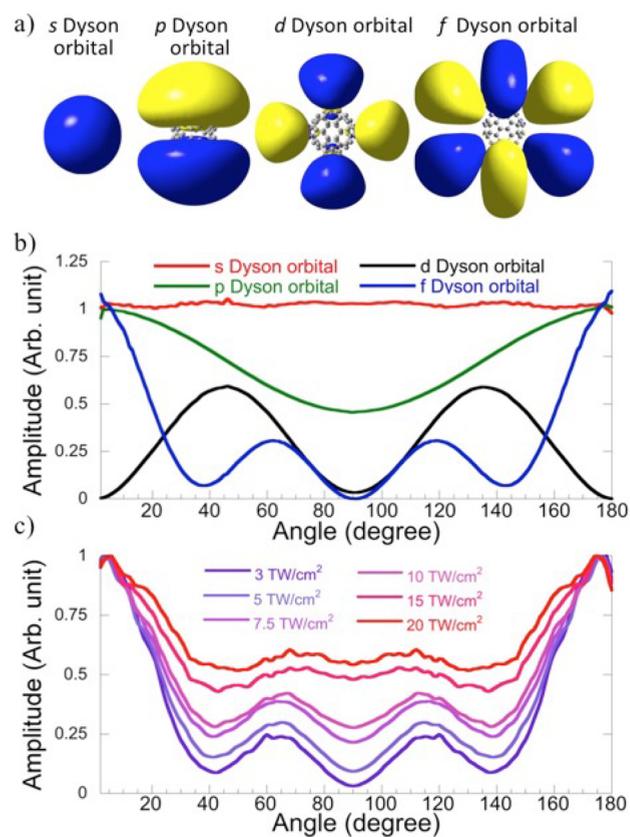
	lifetime (in fs)	
	3 TW/cm <sup>2</sup>	20 TW/cm <sup>2</sup>
p-SAMO	3.48	0.49
d-SAMO	4.58	0.64
2p-Rydberg	9.25	1.31
average on the rydberg series	37.56	5.31

<sup>a</sup>The mean lifetime of the Rydberg states, computed as the average over the 17 bands of Rydberg states present in the TDDFT computation, is also shown for comparison.

of a large band of Rydberg states. For a laser intensity of 20 TW/cm<sup>2</sup>, both SAMO and Rydberg states have lifetimes shorter than 6 fs (Figure 3b). The density of Rydberg states is significantly larger than that of the SAMO states, which is reflected by the broad and intense peak observed experimentally. The lowest energy peak at around 0.2 eV first increases and then decreases with increasing laser intensity and is strongest at around 5.0–10 TW/cm<sup>2</sup> with about 3 times higher peak signal. This trend may be qualitatively understood by the excitation dynamics. When the field is very low, the p-SAMO states, which are lower in energy, should have a larger population than the higher d-SAMO or Rydberg states. As the field strength increases but still is not too strong, the peak grows with population of the p-SAMO state. At higher intensities, all states are populated and the relative height of the p-SAMO peak decreases.

The experimental conditions in our work are similar to those in refs 13, 24, and 36. However, the six-lobe angular distributions for electrons below 0.2 eV have not been reported. The angular distribution can only be clearly observed for low laser intensities and with sufficient signal-to-background ratio. Here, by using a very short pulse duration and low laser intensity, thermal electron emission can be significantly suppressed,<sup>19</sup> as can be seen by the signal in the direction perpendicular to the laser polarization (cf. Figure 1). In contrast, in earlier work,<sup>24</sup> NIR pulses with about 100 fs duration were used to investigate the ionization from SAMO states of  $C_{60}$ . On the time scale of 100 fs, significant nuclear motion, for example via the ag(1)-breathing mode with a period of about 100 fs,<sup>15</sup> may play a role and influence the observations by redistribution of the population from optically active states to the SAMO states.

We now turn to the potential origin of the observed six-lobe photoelectron angular distribution (PAD) at low kinetic energy (see Figure 1a). If this contribution comes from photoionization of a p-SAMO (for a representation of the Dyson orbitals of s-, p-, d-, and f-SAMOs, see Figure 4a), the final angular distribution should be a superposition of s and d distributions,<sup>32</sup> which cannot explain the six-lobe pattern. The six-lobe structure can also not originate from single-photon ionization from an f-SAMO state as proposed in ref 37 because the corresponding PAD should in this case be a superposition of d and g orbitals.<sup>38–41</sup> For the intensities used here, the Stark shift, computed to the second order using  $C_{60}$ 's quadrupole moments (the dipole moment is zero in the neutral and cationic ground states), varies between 0.02 and 0.21 eV for a laser intensity varying between 3 and 20 TW/cm<sup>2</sup>, respectively, which means that several bands of shallow Rydberg states can ionize over the barrier; see Figure 3. Among the 500 excited



**Figure 4.** (a) Isocontour amplitude of the Dyson orbitals of a s-, p-, d-, and f-SAMO or Rydberg states. (b) The angular distributions for the Dyson orbitals from (a). (c) Measured PAD from  $C_{60}$  (0.1–0.2 eV) for laser intensities ranging from 3 to 20 TW/cm<sup>2</sup> as indicated.

states computed in TDDFT, there is a band of f-, d-, and p-Rydberg states with binding energies of 0.01, 0.08, and 0.16 eV, respectively. In this strong-field ionization process, the PAD corresponds to the angular distribution of the orbitals from which the electron is ionized.<sup>38</sup> Because the barrier is lowered more in the field direction, the ionization probability will be larger along the polarization direction. The unique six-lobe PAD can therefore be attributed to OTB ionization from an f-Rydberg state. The energy-integrated PAD for the range of 0.1–0.2 eV at intensities varying from 3 to 20 TW/cm<sup>2</sup> are plotted in Figure 4c. The intensity of the peaks at 60 and 120° increases with the laser intensity because of the isotropic thermal electron emission that also increases with the laser intensity. The agreement of the energy-integrated PAD (for a laser intensity of 3 TW/cm<sup>2</sup>, where thermal contributions are smallest) with the computed angular distribution of an f orbital (Figure 4b) is excellent in terms of both amplitudes and peak locations, and only small angle offsets can be seen. The separation between the two humps of the f orbital is about 60°, while the measured one is about 50°. The small shift could arise from the Coulomb interaction between the ejected electron and the fullerene cage and/or be due to the extra contribution of a d-type angular distribution from the photoionization of a partly overlapping p-SAMO.

To summarize, we have studied the transition from SAMO to Rydberg state photoionization from  $C_{60}$  fullerenes in intense 20 fs laser fields. By comparison with TDDFT calculations, the peaks between 0.2 and 1.5 eV in the PES can be assigned to ionization from p- and d-SAMOs and Rydberg states. The

intensity dependence is interpreted with the photoionization lifetimes of SAMO and Rydberg states, which are selectively ionized when changing the laser intensity. The spectra at low laser intensity are dominated by a peak at kinetic energies below 0.2 eV, which exhibits a six-lobe pattern in the momentum distribution. We interpret the origin of the peak as OTB from f-Rydberg states. Our general findings about the transition from SAMO to Rydberg ionization should also apply to other fullerenes and can help to improve understanding of the photoionization of complex multielectron systems.

## ■ ASSOCIATED CONTENT

### ● Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpcllett.6b02139.

The Supporting Information contains details of the experimental setup and excitation mechanisms of the SAMO and Rydberg states (PDF)

## ■ AUTHOR INFORMATION

### Corresponding Authors

\*E-mail: [matthias.kling@lmu.de](mailto:matthias.kling@lmu.de) (M.F.K.).

\*E-mail: [fremacle@ulg.ac.be](mailto:fremacle@ulg.ac.be) (F.R.).

### Notes

The authors declare no competing financial interest.

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