OPTICS

Multi-octave, CEP-stable source for high-energy field synthesis

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The development of high-energy, high-power, multi-octave light transients is currently the subject of intense research driven by emerging applications in attosecond spectroscopy and coherent control. We report on a phase-stable, multi-octave source based on a Yb:YAG amplifier for light transient generation. We demonstrate the amplification of a two-octave spectrum to 25 μJ of energy in two broadband amplification channels and their temporal compression to 6 and 18 fs at 1 and 2 μm, respectively. In this scheme, due to the intrinsic temporal synchronization between the pump and seed pulses, the temporal jitter is restricted to long-term drift. We show that the intrinsic stability of the synthesizer allows subcycle detection of an electric field at 0.15 PHz. The complex electric field of the 0.15-PHz pulses and their free induction decay after interaction with water molecules are resolved by electro-optic sampling over 2 ps. The scheme is scalable in peak and average power.

INTRODUCTION

Controlling, shaping, and measuring the electric field of light at terahertz frequencies opened new possibilities for a variety of applications from fundamental science to real-world applications (1). Their extension to petahertz frequencies has enhanced the depth of our insight into microscopic ultrafast dynamics at femtosecond and attosecond time scale. It was the controlling of the slippage of the electric field of light relative to its envelope [carrier-envelope phase (CEP) stability] that paved the way for isolated attosecond pulse generation (2). Nowadays, attosecond extreme ultraviolet (XUV) pulses are generated routinely in laboratories and allow control and observation of electron dynamics (3–7). Nevertheless, attosecond metrology and spectroscopy have been restricted to the use of low-energy attosecond XUV pulses in combination with strong few-cycle near-infrared (NIR) fields (8). Pushing the frontiers of attosecond spectroscopy to new areas such as XUV-pump/XUV-probe spectroscopy (9, 10) or attosecond x-ray diffraction (11) to capture the four-dimensional microscopic dynamics of electrons outside the atomic core (12) calls for isolated XUV or x-ray attosecond pulses with sufficient yield. Recently, there has been growing interest in the development of high-energy, long-wavelength, few-cycle lasers (13, 14), as the cutoff energy in high-order harmonic generation (HHG) scales linearly with the peak intensity and quadratically with the wavelength of the driving pulse. However, the harmonic yield at longer wavelength is markedly reduced due to the higher quantum diffusion and lower recombination probability (15–18).

In parallel, many research studies have focused on enhancing the photon flux in HHG by optimizing the shape of the driving field (19–21). It has been theoretically shown that light transients are superior to few-cycle pulses in pushing the frontiers of HHG toward x-rays with higher harmonics yield (4, 22, 23). Here, the presence of the longer wavelengths in the driving field furnishes the recolliding

electrons with more energy. As the multi-octave field is confined to a single field cycle, the pre-ionization of the atoms is reduced (24). Moreover, tailoring the spectral chirp of the light transient allows better control of tunneling ionization and subsequent electronic motion.

Light transients with tens of microjoules of energy have been generated by spectral shaping or field synthesis of multi-octave pulses (25–27). However, increasing their energy to multi-millijoule at several kilohertz repetition rates calls for a power- and energy-scalable scheme (28, 29). Optical parametric chirped-pulse amplifiers (OPCPAs) are capable of delivering few-cycle pulses, scalable in peak and average power. Therefore, coherent combination of few-cycle pulses from multiple broadband OPCPAs allows the generation of light transients with a higher peak and average power (28–31). Here, the energy of few-cycle pulses at different central frequencies is boosted in OPCPA chains before the synthesis of super-octave waveforms via phase-coherent superposition of few-cycle pulses of different carrier frequency. Realizing such a concept requires high-energy lasers to pump and seed several OPCPA chains at different carrier frequencies. Direct generation of the multi-octave, CEP-stable seed spectrum from the pump laser allows intrinsic temporal synchronization between (i) the pump and seed pulses at the OPCPA stages and (ii) different OPCPA channels.

On the basis of this scheme, in 2018, Rossi et al. (32) boosted the energy of the light transients to nearly 1 mJ by using a 20-mJ, 1-kHz, 150-fs Ti:Sa amplifier to (i) generate multi-octave seed pulses and (ii) pump the two parallel OPCPA channels. In a follow-up experiment, Mainz et al. (33) demonstrated the effect of the shape of the generated light transients on HHG yield. However, boosting the energy and average power of light transients beyond this value calls for a different frontend due to the limitations of simultaneous energy and power scalability in Ti:Sa amplifiers (34).

Yb:YAG lasers in thin-disk and slab geometries are capable of delivering pulses at high energy and average power simultaneously (35–37). Between the two, the simultaneous scaling is more optimum in thin-disk lasers due to the efficient heat removal from the typically 100-μm-thick gain medium, which is mounted on a water-cooled diamond substrate. These unique properties in combination with the reliability of industrial diode pumps make Yb:YAG lasers potential

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drivers for high-energy, high-average power light transients. However, their narrowband emission cross section (38), in addition to the gain narrowing, limits their pulse duration to around 1 ps at hundreds of millijoule energy and tens of picoseconds at joule energy (37, 39). Their long pulse duration makes the direct generation of multi-octave, CEP-stable pulses from Yb:YAG more challenging in comparison to Ti:Sa technology.

In what follows, we demonstrate an all-Yb:YAG multi-octave, frontend to pump and seed two OPCPA channels and their temporal compression to few-cycle pulses. We show that the intrinsic synchronization in this scheme reduces the temporal jitter only to long-term drift. The spatial and temporal stability of the synthesizer are confirmed by resolving the electric field of the free induction decay (FID) of water molecules with subcycle temporal resolution.

## RESULTS

Mid-infrared and near-infrared OPCPAs

A schematic of the frontend is depicted in Fig. 1. A homebuilt, Kerr-lens mode-locked Yb:YAG thin-disk oscillator, delivering 2-µJ, 350-fs pulses at 15 MHz, is used to seed a homebuilt, Yb:YAG thin-disk regenerative amplifier (40). The amplifier operates in chirped-pulse amplification configuration. Therefore, the seed pulses are temporally stretched to 2 ns in a pair of gold gratings before amplification and compressed to their Fourier transform limit after the amplification. The laser delivers 20-mJ, 1-ps pulses at 5-kHz repetition rates and serves as the only laser in the synthesizer.

Pump energy (1.8 mJ) is used to generate a CEP-stable, multi-octave, broadband spectrum (41). The resultant supercontinuum spans from 500 to 2500 nm (red curve in Fig. 2A) with 90-mrad root mean squared CEP fluctuations over 100-min measurement time. A broadband dielectric beam splitter (42) is used to divide the seed spectrum into two portions: (i) NIR region from 700 to 1400 nm and (ii) mid-infrared (MIR) region with spectral coverage from 1600 to

2500 nm. The remaining energy of the Yb:YAG amplifier is frequency-doubled in a 0.5-mm-thick type I barium borate (BBO) crystal at a peak intensity of 80 GW/cm^2. The second-harmonic module delivers 9-mJ pulses at 515 nm. Thereafter, the second-harmonic pulses are separated from the fundamental using a dielectric beam splitter.

A single-stage, noncollinear OPCPA containing a 4-mm-thick lithium triborate [LiB$_3$O$_5$ (LBO)] crystal is used to amplify the NIR region of the spectrum. The pump pulses (0.8 mJ) at 515 nm are focused to an 850-µm beam diameter [full width at half maximum (FWHM)], slightly larger than the 650-µm (FWHM) seed beam. Pump and seed beams are crossed at an internal angle of 1.05° inside the LBO crystal with the phase-matching angle of φ = 15° in type I configuration. The amplified spectrum with 20 µJ of energy is shown in Fig. 2A (orange curve). Afterward, the amplified beam is collimated and sent through a custom-designed chirped-mirror compressor. The compressor consists of 16 double-angle chirped mirrors with a group delay dispersion of −30 fs^2 per bounce and a pair of thin fused-silica wedges at the Brewster angle for fine dispersion control. A second-harmonic frequency-resolved optical gating (SH-FROG) containing a 10-µm-thick BBO crystal is used to characterize the compressed pulses. Figure 2B shows the measured and retrieved spectrograms and the retrieved temporal intensity profile and phase of the compressed pulses to 6 fs (FWHM).

After separation using the dielectric beam splitter, the MIR seed pulses pass through an acousto-optic programmable dispersive filter (Fastlite, Dazzler) and amplified in a single-stage degenerate OPCPA containing a 2-mm-thick periodically poled lithium niobate crystal with a poling period of 30.64 µm. Pulses (180 µJ) at 1030 nm with a peak intensity of 70 GW/cm^2 are used to pump the MIR-OPCPA stage. The angle (1°) between the seed and pump beams is induced to facilitate the separation of the signal beam after amplification. Figure 2A (brown curve) shows the spectrum of the 5-µJ amplified MIR pulses. The amplified pulses were compressed to 18 fs by using a 2-mm-thick silicon in combination with the introduced phase by
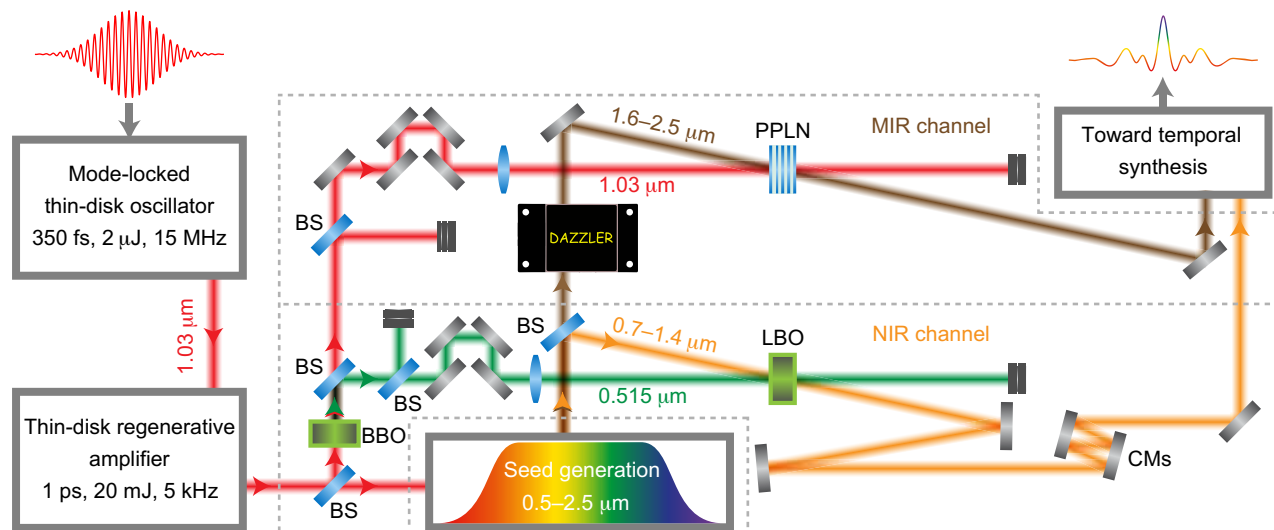
Fig. 1. All-ytterbium frontend for high-average and peak power light transient generation. The setup is based on a Yb:YAG thin-disk amplifier, seeded by a Kerr-lens mode-locked thin-disk oscillator. The laser energy (1.8 mJ) is used to directly generate multi-octave, CEP-stable seed pulses. Thereafter, the broadband spectrum is divided into two channels: NIR channel spanning from 700 to 1400 nm and MIR channel covering 1600 to 2500 nm. Each channel is amplified in a single-stage OPCPA pumped by fundamental or second harmonic of the laser and compressed to its Fourier limit. The energy of few-cycle pulses can be increased by adding consecutive OPCPA stages in each channel. Coherent synthesis of the two few-cycle pulses results in generation of light transients. BS, beam splitter; CMs, chirped mirrors; PPLN, periodically poled lithium niobate.
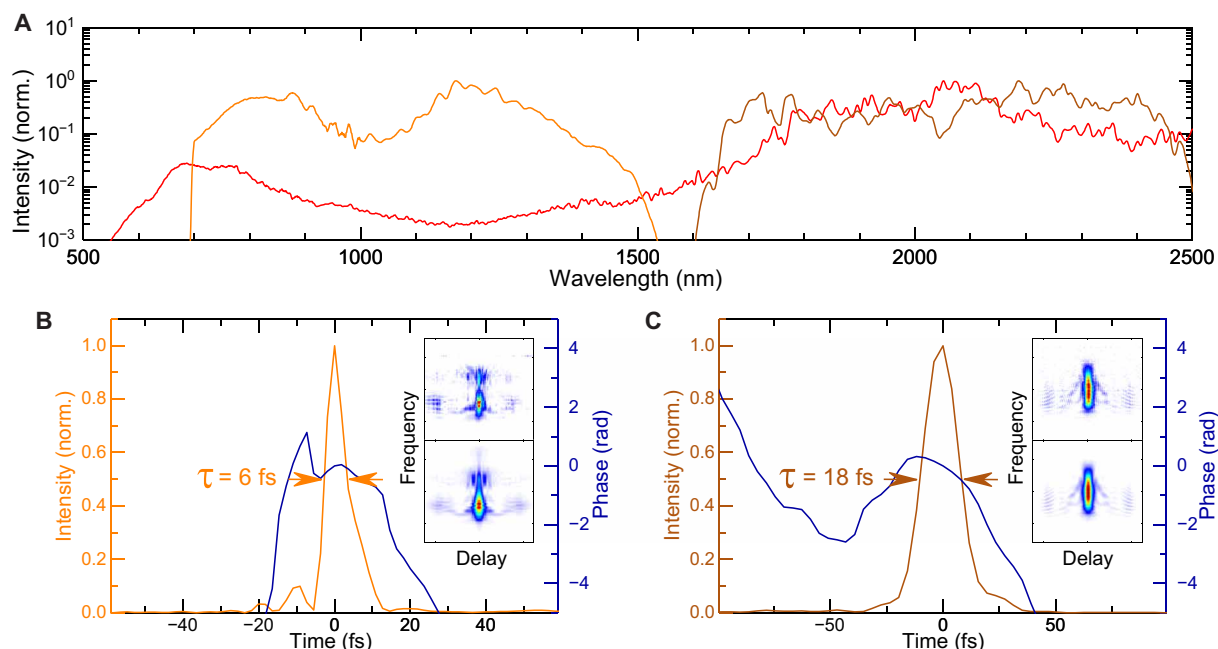
Fig. 2. The laser specifications. (**A**) CEP-stable, multi-octave spectrum of seed pulses (red). Amplified spectra of NIR (orange) and MIR (brown) OPCPAs. Retrieved temporal intensity profile and phase of the compressed pulses in (**B**) NIR and (**C**) MIR channels. Inset: Measured (top) and retrieved (bottom) FROG spectrograms.

Dazzler. Figure 2C shows the measured and retrieved spectrograms and the retrieved temporal intensity profile and phase of the MIR pulse. These measurements were done by an SH-FROG containing a 100-μm-thick BBO crystal.

Temporal and phase jitter

Combining the MIR and NIR few-cycle pulses by using a broadband dielectric beam combiner and their coherent superposition leads to the generation of light transients. In few-cycle coherent synthesis, the relative temporal overlap between the few-cycle pulses results in a great variety of light transients (*23*). Therefore, as with any kind of interferometer, relative phase and relative timing between the two arms of the synthesizer define the ultimate stability of the generated light transient (*43*, *44*). In our scheme, the CEP stability of the seed pulses results in the stability of the absolute phase of both OPCPA channel outputs. Moreover, the direct multi-octave seed generation from the pump laser ensures the intrinsic temporal synchronization and restricts the temporal jitter only to long-term drift. To avoid any temporal instability caused by fluctuations in the arrival of pump pulses in each OPCPA channel, we kept the seed pulse duration shorter than the pump pulse duration. This approach allows decoupling of the nonlinear amplification process from linear temporal jitter between the seed and pump pulses and restricts temporal jitter to long-term drifts caused by the optical path of the synthesizer.

As the few-cycle pulses from both OPCPAs contain only 2 to 3 cycles of electric field, the temporal jitter between the two channels has to be lower than a fraction of their half-field cycle. To prove the intrinsic synchronization between the two channels over a time window of several picoseconds and restriction of the temporal jitter to long-term drifts, we conducted an experiment with the new source.

Upon the interaction of broadband pulses with molecules, photons at the resonance frequencies are slowed down because of the increase in the refractive index and appear at the trailing edge of the

excitation pulse. The delayed response, which is called FID (*45*), can be explained by the Kramers-Kronig relation and lasts for several picoseconds in liquid phase. We aimed for the direct electric field detection of the MIR pulses and their FID after interaction with water molecules over several picoseconds by means of electro-optic sampling (EOS) (*46*). The NIR pulses are used as probe pulses in EOS and are required to have a temporal jitter below the subcycle duration of the MIR pulses over the entire scanning range to allow resolution of the fast oscillating electric field of the MIR pulses and the FID.

Direct electric field sampling

We chose to detect water's molecular response, as water has a strong $\nu_2 + \nu_3$ combination band near 1930 nm (5180 cm^{-1}) (*47*). The 18-fs MIR pulses were used to excite the combination band and were focused using a 4-inch focal length off-axis parabolic mirror into deionized water sandwiched between two 2.3-mm-thick sapphire windows with 500-μm spacing. Afterward, the transmitted beam was collimated using another 4-inch focal length off-axis parabolic mirror and sent to the EOS setup for field detection (see Fig. 3A).

The EOS setup is illustrated in Fig. 3B. The 6-fs NIR pulses are collinearly combined with the transmitted MIR pulses from the sample in a broadband wire grid polarizer (Thorlabs, WP25L-UB) and focused into a 50-μm-thick BBO crystal at the phase-matching angle of θ = 25° for type II sum-frequency generation. The sum-frequency signal at 670 nm has orthogonal polarization relative to the NIR probe pulses. To enhance the detection sensitivity, the spectral range between 650 and 750 nm of the transmitted beams after the BBO crystal is filtered out (*48*). The interference between the NIR probe pulses and the sum-frequency signal is assured by a quarter-wave plate. The resulted polarization rotation is read out using an ellipsometer consisting of a Wollaston prism and balanced photodiodes as a function of relative timing of the NIR and MIR pulses. The MIR pulses
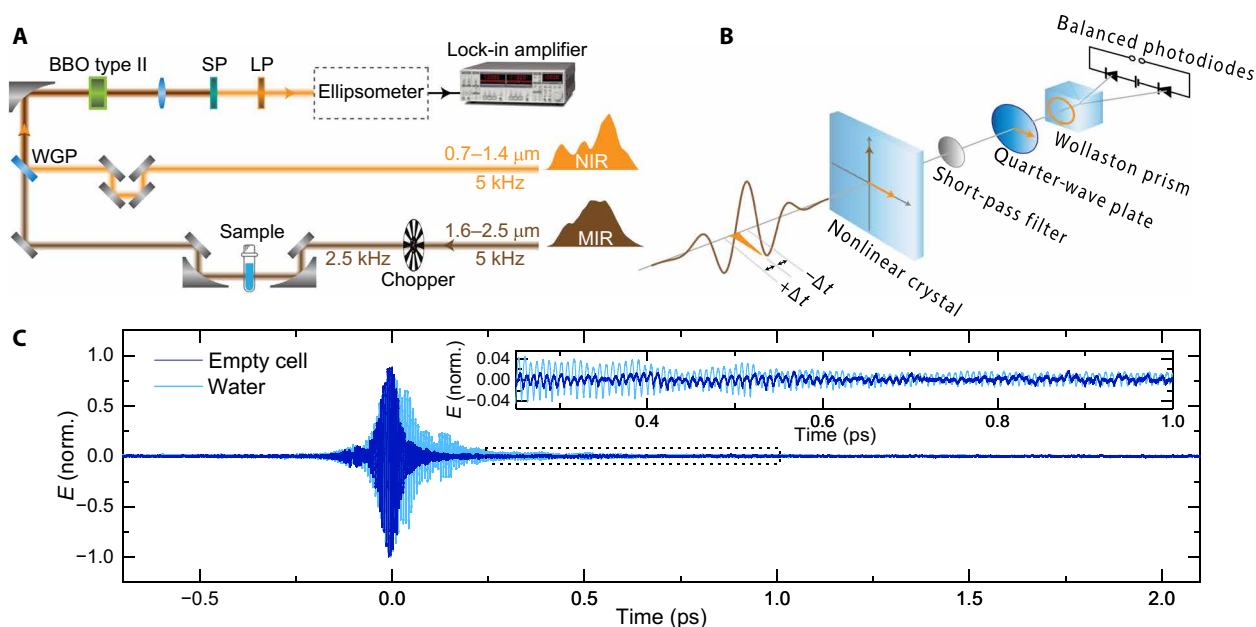
Fig. 3. Direct electric field detection. (A) Schematic of the linear absorption setup for generating and sampling the FID of water molecules. **(B)** EOS setup containing a 50-µm-thick BBO (type II) crystal and an ellipsometer. The MIR pulses are chopped at 2.5 kHz. The NIR beam after the delay line is collinearly combined with the MIR beam, and both are focused in the EOS crystal for sum-frequency generation. The generated sum-frequency signal spectrally overlaps and temporally interferes with the high-frequency components of the probe beam. Appropriate spectral filtering is used to enhance the EOS signal. The polarization rotation as a function of time delay is detected using an ellipsometer and read out using a lock-in amplifier. **(C)** Measured electric field of the MIR pulses in the absence (dark blue curve) and presence of water (light blue curve). Inset: Zoomed plot in a shorter temporal window. WGP, wire grid polarizer; SP, short-pass filter; LP, long-pass filter.
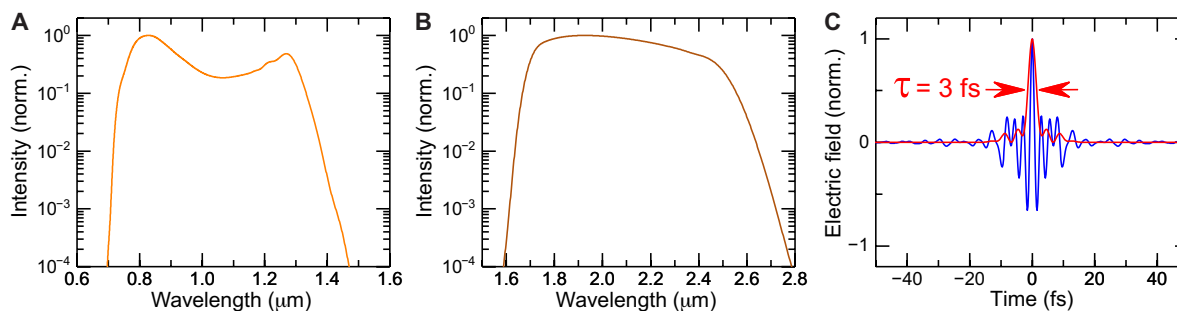
Fig. 4. Simulated millijoule light transient. Simulated amplified spectra in **(A)** NIR channel with 1.8 mJ of energy and **(B)** MIR channel with 2.2 mJ of energy and **(C)** their calculated synthesized waveform.

are modulated at 2.5 kHz with a mechanical chopper, while the mechanical delay stage was tracked (*49*).

Figure 3C shows the measured electric field of the MIR pulses in the absence (dark blue curve) and presence (bright blue curve) of water. To probe the MIR pulses, we scanned the delay stage in the probe channel over 450 µm with a speed of 1.7 µm/s, corresponding to a single-shot detection at each delay position. As can be seen, in the absence of water, the amplitude of the excitation pulses goes to zero at temporal delays above 200 fs. After the injection of water, the transmitted excitation pulse is temporally chirped and the molecular free induction decay (FID) is formed. Resolving the electric field of the MIR pulses with subcycle precision over a 3-ps time window and in the absence of active stabilization demonstrates the spatial and temporal stability of the synthesizer.

Moreover, here, the molecular response can be detected free of background at temporal delays beyond 200 fs, allowing higher detection sensitivity. By using broadband excitation pulses in com-

bination with EOS, the entire molecular vibrations in the fingerprint region can be simultaneously excited and detected, which holds promise for advancing femtosecond time-domain spectroscopy to direct measurement of the complex electric field and higher detection sensitivity.

DISCUSSION

In summary, we demonstrated an all-ytterbium source for high-energy light transient generation based on OPCPA. The frontend covers a spectral range from 700 to 2500 nm and delivers intrinsically synchronized 6- and 18-fs pulses with a total energy of 25 µJ at 5-kHz repetition rates. The source is capable of delivering subcycle light transients with 3-fs temporal duration. The stable CEP was ensured by generating passively CEP-stable multi-octave seed pulses directly from the Yb:YAG amplifier. The temporal jitter between the NIR and MIR pulses in this scheme is only dominated by long-term drift.

Table 1. Simulation parameters of the NIR channel. L_c, crystal thickness; E_p, input pump energy; E_s, amplified signal energy; ω_p, pump beam radius (FWHM); ω_s, signal beam radius (FWHM).

Stage	L_c (mm)	E_p (mJ)	E_s (mJ)	ω_p (mm)	ω_s (mm)	Efficiency (%)
2nd	2.5	8.3	1.3	1.46	1.16	15.1
3rd	1.0	6.0	1.8	1.28	1.02	9.8

Table 2. Simulation parameters of the MIR channel.

Stage	L_c (mm)	E_p (mJ)	E_s (mJ)	ω_p (mm)	ω_s (mm)	Efficiency (%)
2nd	2.0	8.9	1.3	1.63	1.50	14.9
3rd	1.0	6.2	2.2	1.42	1.34	13.9

As a first application, we demonstrated the direct measurement of the transmitted electric field of the MIR pulses after interaction with water with subcycle resolution. The linear absorption of the MIR pulses by water molecules forms an FID at the trailing edge of the MIR pulses that lasts for several picoseconds. Few-cycle, NIR pulses were used to probe the oscillating MIR electric field over a 3-ps time window, which proves the relative spatial and temporal stability of the MIR and NIR channels. Moreover, this is the first measurement of the complex electric field of the FID of overtone and combination bands to the best of our knowledge. The demonstrated control and measurement of the electric field of light at 0.5 PHz hold promise to open up new opportunities for precise observation and control of molecular vibrations over the entire molecular fingerprint region down to a few femtosecond time scales.

Multi-millijoule, light transients hold promise for advancing attosecond pulse generation to higher power level and higher photon energies. Our simulations suggest that by using the available pump energy in additional amplifier stages, the energy of the two-octave spectrum can be scaled to 4 mJ (Fig. 4). Higher energy and average power can be achieved by using a 5-kW, 200-mJ Yb:YAG amplifier (37) as the driving laser.

MATERIALS AND METHODS

The presented three-dimensional simulations in Fig. 4 were performed using SISYFOS (Simulation System For Optical Science) (50). In this code, optical parametric frequency conversions in nonlinear media were simulated by using a Fourier space method. SISYFOS solves the coupled differential equations for the slowly varying amplitudes. This model can take into account most of the relevant physical effects in the frequency conversion such as propagation effects, second- and third-order nonlinearity, thermal effects, two-photon absorption, and noncollinear interactions. In this numerical simulation, we neglected the thermal effects, third-order nonlinear processes, and two-photon absorption. The Sellmeier coefficients were obtained from (51, 52). For simulating the NIR channel, the amplified spectrum in the first stage (orange curve in Fig. 2A) was further amplified into two additional amplification stages. The remaining energy (8.3 mJ) from the second-harmonic module at 515 nm was used to pump the second stage

and recycled at the third amplification stage. The pump beam size was adjusted to keep its peak intensity at 100 GW/cm^2. The parametric amplification was formed in an LBO crystal with a phase-matching angle of 15.5°, an internal noncollinear angle of 1.05°, and d_{eff} = 0.82 pm/V, resulting in the amplified pulse energy of 1.8 mJ. The detailed parameters of the NIR chain are summarized in Table 1.

For simulating the amplified spectrum of the MIR channel (brown curve in Fig. 2A), 8.92 mJ of pump energy at 1030 nm was used to pump two OPCPA stages, while the pump energy was recycled at the last stage. The pump intensity in all stages was set to 70 GW/cm^2. The signal energy was boosted to 2.2 mJ in the MIR chain by using a type I lithium niobate (LiNbO$_3$) crystal with a phase-matching angle θ = 42.9° and assumed d_{eff} value of 3.96 pm/V. Table 2 summarizes the simulation parameters of the MIR channel.

SUPPLEMENTARY MATERIALS

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/6/7/eaax3408/DC1

Table S1. Simulation parameters of the NIR channel.
Table S2. Simulation parameters of the MIR channel.

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Acknowledgments